

Booklet # 45



Unit: Work || Topic: Hooke's Law
Date: Dec 14, 2015 || Name:



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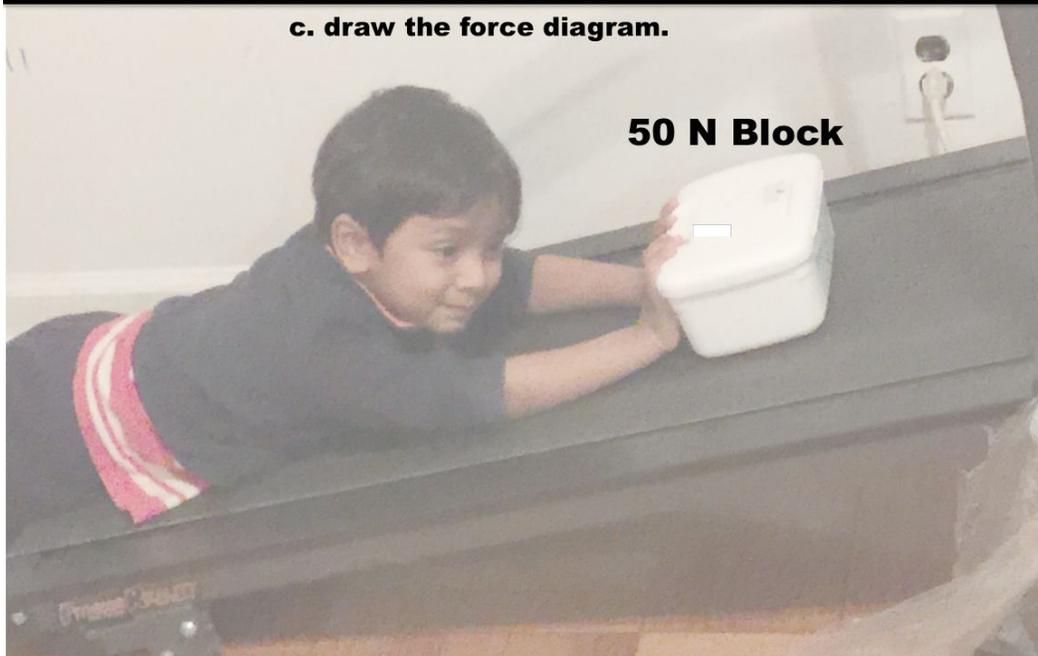
Inclined plane

A 50 N block is placed on a frictionless 20 degree incline.

a. Find net force acting on it?

b. Find acceleration of the block

c. draw the force diagram.

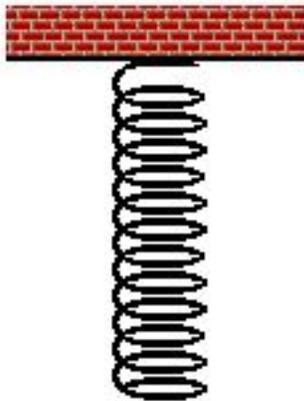


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Motion of a Mass on a Spring

We will begin our discussion with an investigation of the forces exerted by a spring on a hanging mass.

Consider the system shown below with a spring attached to a support. The spring hangs in a relaxed **unstretched** position.



A coiled spring in its relaxed position.

If you were to hold the bottom of the spring and pull **downward**, the spring would **stretch**.

If you were to pull with just a little force, the spring would **stretch** just a little bit. And if you were to pull with a much greater force, the spring would stretch a much greater extent.

Exactly what is the quantitative relationship between the amount of **pulling force** and the **amount of stretch**?

To determine this quantitative relationship between the amount of **force** and the amount of **stretch**, objects of known **mass** could be attached to the **spring**.

For each object which is added, the amount of **stretch** could be measured. The force which is applied in each instance would be the **weight** of the object.

A regression analysis of the force-stretch data could be performed in order to determine the quantitative relationship between the **force** and the amount of **stretch**. The data table below shows some representative data for such an experiment.

| Mass (kg) | Force on Spring (N) | Amount of Stretch (m) |
|------------------|----------------------------|------------------------------|
| 0.000 | 0.000 | 0.0000 |
| 0.050 | 0.490 | 0.0021 |
| 0.100 | 0.980 | 0.0040 |
| 0.150 | 1.470 | 0.0063 |
| 0.200 | 1.960 | 0.0081 |
| 0.250 | 2.450 | 0.0099 |
| 0.300 | 2.940 | 0.0123 |
| 0.400 | 3.920 | 0.0160 |
| 0.500 | 4.900 | 0.0199 |

By plotting the force (X axis) -stretch (y axis) data and performing a linear regression analysis, the quantitative relationship or equation can be determined. The plot is shown below.

The fact that the regression constant is very close to **1.000** indicates that there is a *strong fit* between the **equation** and the **data points**.

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| | <p>This relationship between the force applied to a spring and the amount of stretch was first discovered in 1678 by English scientist Robert Hooke.</p> <p>The amount that the spring extends is proportional to the amount of force with which it pulls.</p> $F_{\text{spring}} = -k \cdot x$ <p>where F_{spring} is the force exerted upon the spring, x is the amount that the spring stretches relative to its relaxed position, and k is the spring constant. The units on the spring constant are Newton/meter (N/m).</p> <p>The negative sign in the above equation is an indication that the direction that the spring stretches is opposite the direction of the force which the spring exerts.</p> |
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Below materials are For regents students only

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| <p>6</p> | <p>Calculus # 1 (Differentiation) Review: (power rule, product rule, quotient rule and chain rule)</p> |
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3. under the curve $y = x^2 - 2x + 8$ from $x = 1$ to $x = 2$